



St Paul's Calculation Policy

September 2022



This policy outlines our clear intention to teach children to develop conceptual understanding through the progression of ***concrete, pictorial and abstract*** methods.

This calculation policy should be used to support children to develop a deep understanding and mastery of number and calculation. We support and extend children as needed, broadening, deepening and applying their calculation knowledge.

Using the concrete-pictorial-abstract approach:

Children develop an understanding of a mathematical concept through the three steps (or representation) of concrete-pictorial-abstract approach. Reinforcement is achieved by going back and forth between these representations.

Concrete representation: The enactive stage - a pupil is first introduced to an idea or a skill by acting it out with real objects. This is a 'hands on' component using real objects and it is the foundation for conceptual understanding.

Pictorial representation: The iconic stage - a pupil has sufficiently understood the hands-on experiences performed and can now relate them to representations, such as a diagram or picture of the problem.

Abstract representation: The symbolic stage - a pupil is now capable of representing problems by using mathematical notation, for example: $12 \div 2 = 6$.

+ Addition



Year	Objective	Concrete	Pictorial	Abstract
3	Add 2 and 3 digit numbers	<p>Modelled with and children using dienes and place value counters</p>	<p>Drawing of dienes and place value counter.</p>	
4	Add any 4 digit number to any 4 digit number.	<p>Exchanging. Make both numbers on a place value grid.</p>	<p>Pictorial representations of columns and place value counters demonstrating regrouping.</p>	
5	Add numbers with more than 4 digits. Add decimals with 2 decimal places, including money.	<p>Introduce decimal place value counters and model exchange for addition.</p>		
6	Add several numbers of increasing complexity including adding money, measure and decimals with different decimal points.			

- Subtraction



Year	Objective	Concrete	Pictorial	Abstract																														
3	Up to 3 digit subtraction with <u>exchanging</u>		<p>Drawing of base ten or PV counters with <u>exchanging</u>.</p>	<p>836 - 254 = 582</p> <p>First with <u>partitioning</u>.</p> <table border="1"> <tr><td>6</td><td>12</td><td></td></tr> <tr><td>7</td><td>2</td><td>8</td></tr> <tr><td>-</td><td>5</td><td>8</td><td>2</td></tr> <tr><td></td><td>1</td><td>4</td><td>6</td></tr> </table> <p>Then formal method.</p>	6	12		7	2	8	-	5	8	2		1	4	6																
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7	2	8																																
-	5	8	2																															
	1	4	6																															
4	Subtract 4 digit numbers.	<p>234 - 179</p> <p>Model process of exchange using Numicon, base ten and then move to PV counters.</p>	<p>Represent the place value counters pictorially; remembering to show what has been exchanged.</p>	<table border="1"> <tr><td></td><td>6</td><td>15</td><td></td></tr> <tr><td>2</td><td>7</td><td>5</td><td>4</td></tr> <tr><td>-</td><td>1</td><td>5</td><td>6</td><td>2</td></tr> <tr><td></td><td>1</td><td>1</td><td>9</td><td>2</td></tr> </table>		6	15		2	7	5	4	-	1	5	6	2		1	1	9	2												
	6	15																																
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5	Subtract with at least 4 digits, including money and measures. Subtract with decimal values.		<p>52.7 - 27.9</p>	<table border="1"> <tr><td></td><td>10</td><td></td><td></td><td></td></tr> <tr><td>6</td><td>7</td><td>16</td><td>8</td><td>10</td></tr> <tr><td>7</td><td>7</td><td>6</td><td>8</td><td>10</td></tr> <tr><td>-</td><td>3</td><td>7</td><td>2</td><td>5</td></tr> <tr><td></td><td>6</td><td>7</td><td>9</td><td>6</td><td>5</td></tr> </table> <p>7169 - 372.5</p> <p>Using zeros as <u>place holders</u></p>		10				6	7	16	8	10	7	7	6	8	10	-	3	7	2	5		6	7	9	6	5				
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6	Subtract with increasingly large and more complex numbers and decimal values.			<table border="1"> <tr><td></td><td></td><td>14</td><td>9</td><td></td><td></td></tr> <tr><td>0</td><td>7</td><td>16</td><td>8</td><td>10</td><td></td></tr> <tr><td>7</td><td>16</td><td>8</td><td>10</td><td>9</td><td>9</td></tr> <tr><td>-</td><td>8</td><td>9</td><td>9</td><td>4</td><td>9</td></tr> <tr><td></td><td>6</td><td>0</td><td>7</td><td>5</td><td>0</td></tr> </table>			14	9			0	7	16	8	10		7	16	8	10	9	9	-	8	9	9	4	9		6	0	7	5	0
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X Multiplication



Year	Objective	Concrete	Pictorial	Abstract
3	Multiply 2 digit by 1 digit.	<p>23x3</p> <p>With place value counters</p>	<p>Children to represent the concrete manipulatives pictorially.</p>	<p>Progression to formal written method.</p>
4	Multiply 2 digit numbers by one digit using formal written method.	<p>Abstract methods from year 3 modelled alongside concrete manipulatives.</p>		<p>expanded method leading to compact method.</p>
5	Multiply 4 digit x 2 digit using long multiplication for 2 digit numbers.	<p>Children can continue to be supported by place value counters at the stage of multiplication.</p>	<p>Pictorial representations (including bar modelling) to support problem solving.</p>	
6	Multiply 4 digit x 2 digit. Multiplying decimals up to 2 decimal places.			

÷ Division



Year	Objective	Concrete	Pictorial	Abstract
3	Divide 2 digit by 1 digit.	<p>Short division using place value counters to group. 615 ÷ 5</p>	<p>Children can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups:</p>	<p>$29 \div 8 = 3 \text{ REMAINDER } 5$</p> <p>↑ ↑ ↑ ↑ dividend divisor quotient remainder</p> <p>$29 \div 8 = 3 \text{ r}5$</p> <p>Introduce remainder sign.</p>
4	Divide 3 digit by 1 digit.	<p>Sharing using place value counters. $42 \div 3 = 14$</p>		<p>Remainders shown as fractions or decimals.</p>
5	Divide 4 digit by 1 digit with remainders.	<p>Divide objects between groups and see how much is left over</p>	<p>Children to represent the lollipop sticks pictorially:</p> <p>There are 3 whole squares, with 1 left over.</p>	<p>Remainders shown as fractions or decimals.</p>
6	Divide 4 digit by 2 digit. (Long division.)			